

# Completeness of Online Planners for Partially Observable Deterministic Tasks

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# Motivation

Many online planners for **partially observable deterministic** tasks  
(e.g. Brafman & Shani 2016, B. & Geffner 2014, Maliah et al. 2014, ...)

Some planners offer **guarantees** over classes of problems

But theoretical analyses are often overly complex and specific to the planners and tasks

Want to develop **general framework** for analysis of online planning

# Model for POD Tasks

Partially observable deterministic tasks correspond to tuples  $P = (S, A, S_{init}, S_G, f, O, \Omega)$  where:

- $S$  is finite state space
- $A$  is finite set of actions where  $A(s)$  is set of actions applicable at  $s$
- $S_{init} \subseteq S$  is set of possible initial states
- $S_G \subseteq S$  is set of goal states
- $f : S \times A \rightarrow S$  is **deterministic transition function**
- $O$  is finite set of observation tokens
- $\Omega : S \times A \rightarrow O$  is **deterministic sensing model**

# Executions and Belief States

Agent sees **observable executions**; an observable execution is a **finite interleaved sequence** of actions and observations:

$$\tau = \langle a_0, o_0, a_1, o_1, \dots \rangle$$

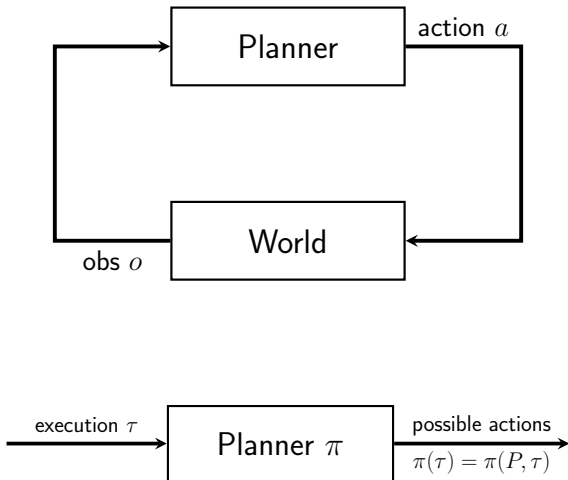
Belief  $b_\tau$  = states deemed possible **after seeing execution**  $\tau$ :

- $b_{\langle \rangle} = S_{init}$
- $b_{\langle \tau, a \rangle} = \{ s' \in S : \text{there is } s \in b_\tau \text{ and } s' = f(s, a) \}$  (progression)
- $b_{\langle \tau, a, o \rangle} = \{ s' \in b_{\langle \tau, a \rangle} : \Omega(s', a) = o \}$  (filtering)

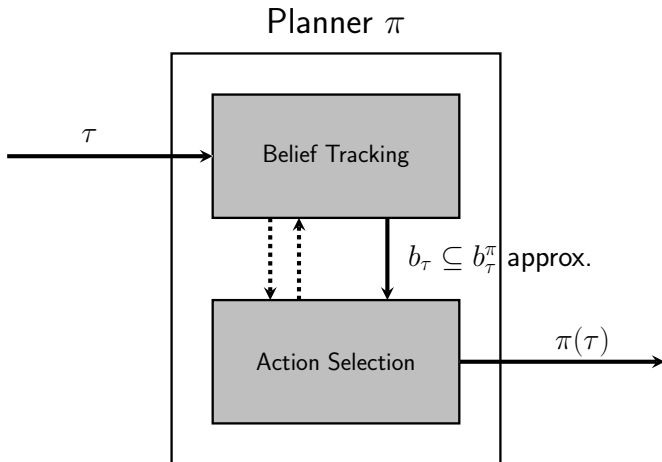
$$b_\tau \xrightarrow{a} b_{\langle \tau, a \rangle} \xrightarrow{o} b_{\langle \tau, a, o \rangle}$$

**Belief tracking on factored models is intractable!**

# Online Planner: Closed-Loop Controller



## Two Components in Online Planners



# Online Protocol

Use of planner in online setting normed/modeled by **protocol**

Protocol  $L = (P, s)$  **determined** by task  $P$  and initial state  $s$ :

1. Let  $\lambda = \langle s \rangle$  be initial **state trajectory** seeded at  $s$
2. Let  $\tau = \langle \rangle$  be empty **execution**
3. While  $b_\tau^\pi \subseteq S_G$  (i.e. agent isn't sure of reaching goal) do
4.     **Run** planner  $\pi$  on input  $\tau$  to obtain set of applicable actions  $\pi(\tau)$
5.     If  $\pi(\tau)$  is empty, terminate with **FAILURE**
6.     **Non-deterministically choose** action  $a \in \pi(\tau)$
7.     Let  $s' := f(\text{Last}(\lambda), a)$  and token  $o := \Omega(s', a)$
8.     **Update**  $\lambda := \langle \lambda, s' \rangle$  and  $\tau := \langle \tau, a, o \rangle$

where  $b_\tau^\pi$  is **approximation** of  $b_\tau$  computed by agent

# Main Goal

Formulate **formal properties** of components and their relation in order to guarantee **completeness** over **solvable tasks**

## Definition (Completeness)

*Online planner  $\pi$  is complete on task  $P$  if for each initial state  $s \in S_{init}$ , the protocol  $L(P, s)$  **terminates successfully** on  $\pi$*

We would like to reason about completeness; e.g.

- Is planner  $\pi$  complete on  $P$ ?
- Why isn't  $\pi$  complete on  $P$ ?
- How do we make  $\pi$  complete on  $P$ ?
- ...



# Solvable Tasks

Two definitions:

## Definition (Solvable Tasks)

*Task  $P$  is **solvable** (or goal connected) if there is a plan for each state  $s$  in  $P$*

## Definition (Strongly Solvable Tasks)

*Task  $P$  is **strongly solvable** (or goal connected in belief space) if for each initial state  $s$  and execution  $\tau$  compatible with  $s$ , there is an extension  $\tau' = \langle \tau, \tau'' \rangle$  compatible with  $s$  such that  $b_{\tau'}$  is a goal belief*

Definitions are **incomparable**: there are tasks that are solvable but not strongly solvable, and vice versa

# Reasons for Incompleteness

- Belief tracking is too weak; i.e. approximation  $b_{\tau}^{\pi}$  of  $b_{\tau}$  is too coarse
- Action selection is bad or **uncommitted**
- Combination of belief tracking and action selection isn't good enough

## Uncommitted Planner Fails in Simple Example



- Agent is thirsty and wants a drink; it can move and gulp a drink
- There are two drinks
- No need for belief tracking as state is always known
- Agent may loop even if selected action always moves “toward goal” (e.g. Left, Right, Left, Right, ...)

# Properties for Belief Tracking

- **Exact:** beliefs computed by  $\pi$  are **exact**; i.e.,  $b_{\tau}^{\pi} = b_{\tau}$  for each  $\tau$
- **Monotone:** for every execution  $\tau$  and **prefix**  $\tau'$  of  $\tau$ ,  $|b_{\tau}^{\pi}| \leq |b_{\tau'}^{\pi}|$  (i.e. non-increasing “amount of uncertainty” along executions)
- **Asserting:** there is asserting inference for pair  $(\tau, \tau')$  (where  $\tau'$  is **proper prefix** of  $\tau$ ) if  $|b_{\tau}^{\pi}| < |b_{\tau'}^{\pi}|$  (uncertainty decreases)

Exact inference  $\implies$  monotone inference (because determinism)

## Properties for Action Selection

For handling commitment, we do a slight reformulation and consider planners that return set of **action sequences (plans)** on input  $\tau$

First action on each sequence  $\sigma$  **must be applicable**

Properties:

- **Committed:** by caching last computed sequences, the planner sticks to selected plan “as much as possible”
- **Weak:** for each approximation  $b^\pi$ :
  - each sequence  $\sigma$  returned by  $\pi$  is a **plan for some state**  $s \in b^\pi_\tau$
  - if  $b^\pi_\tau$  is non-empty,  $\pi$  returns at least one sequence  $\sigma$
- **Covering:** the first action in sequences returned by  $\pi$  **cover all** applicable actions at **exact belief**  $b_\tau$

## Relation between Components

Do we need **exact but intractable** belief tracking for completeness?

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**Fortunately not!**

A **sufficient** condition:

- Planner  $\pi$  is **weak**: given execution  $\tau$ ,  $\pi$  returns at least one plan  $\sigma$  for some state  $s \in b_{\tau}^{\pi}$  (state  $s$  may not be in  $b_{\tau}$ )
- Plan  $\sigma$  is applied while possible (i.e. **committed planner**)
- Belief tracking is **monotone**
- Planner is **effective**: if executed prefix of  $\sigma$  doesn't reach goal, planner  $\pi$  has **asserting inference** for  $(\tau[\sigma], \tau)$

# Main Formal Result

## Theorem

Let  $P$  be a **solvable task** and  $\pi$  be a **committed planner**. If  $\pi$  is a **weak and effective**, and has **monotone inference**, then  $\pi$  is **complete** for  $P$ .



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*Sketch:* For each protocol  $L = (P, s)$ , planner in worst case generates a **sequence of beliefs** (associated to ongoing execution):

$$b_0^\pi \supseteq b_1^\pi \supseteq b_2^\pi \supseteq \dots \supseteq b_n^\pi = \{s^*\}$$

that ends at **singleton**. Once there, since  $\pi$  is weak and committed,  $\pi$  generates and applies a plan for the current hidden state  $s^*$  QED

## Another Result

Under **randomized protocols** where action selection is **stochastic** instead of just **non-deterministic**:

### Theorem

*Let  $P$  be a **strongly solvable** task with **observable goals** and  $\pi$  be a planner. If  $\pi$  is a **covering planner**, then  $\pi$  is complete under randomized protocols*

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*Sketch:* Since task is strongly solvable, there is always a plan from current belief. Under assumptions, this plan can be “followed” with **non-zero probability**. Upon reaching a goal state, the agent will know it since goals are observable QED

**Remark:** there is no need for  $\pi$  to be weak or committed, or to have exact inference; it has to be covering though!

# Experimental Results

**See paper for details and experimental results on benchmarks**

# Wrap Up

- Framework for understanding and reasoning about online planning
- Preliminary theoretical results
- Played with planner LW1
- Future work:
  - Study necessary conditions for completeness
  - “Effectiveness” cannot be tested in an efficient manner
  - Novel action selection mechanisms
  - Novel tractable belief tracking methods

**Lot of ground breaking work to be done in the area**